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A Novel Approach to the Development of Linear Elliptic Solvers

by

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Abstract

This study is concerned with the development of accurate and efficient techniques for solving linear elliptic systems such as the Laplace and Lamé equations in three-dimensional domains. The methodology is investigated in the context a Galerkin boundary integral equation approach with both singular and hypersingular formulations. Taking the 3D Laplace equation as the example to discuss the algorithm, surface integrals are defined as limits to the boundary and linear surface elements are employed to approximate the geometry and boundary functions. In the inner integration procedure, it is shown that all singular and non-singular integrals over a triangular boundary element can be expressed exactly as a sum of analytic formulae over the sides of the designated element. It is also established that weakly-singular, strongly-singular and hypersingular integrals are simply special cases of non-singular integrals. In the outer integration scheme, closed-form expressions are obtained for the coincident case, wherein the divergent hypersingular terms are identified explicitly, and shown to cancel with corresponding terms from the edge-adjacent case. The remaining edge-adjacent, vertex-adjacent and non-coincident integrals contain only weak singularities and can be carried out easily by use of suitable numerical cubature. This semi-exact treatment does not seem to suffer from the usual inaccuracies associated with near-singular (or quasi-singular) integrals; i.e., integrals over a pair of triangular elements that are "very close". The semi-analytic method is further accelerated by a Fast-Fourier-Transform-based matrix compression technique to achieve a significant reduction in execution time and memory requirements over standard approaches. The performance of the proposed algorithm is illustrated with several numerical examples.

Time: 12:05 - 12:55 pm

Date: Friday, October 12th, 2007

Room: Mason 142A

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